



## SEMINARIUM MATEMATYKA DYSKRETNA

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### Polowanie na pająki o długich nogach

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Hons, Klimošová, Kucheriya, Mikšaník, Tkadlec, and Tyomkyn proved that, for every integer  $\ell \geq 1$ , every directed graph with minimum out-degree at least  $3.23 \cdot \ell$  contains a  $(2, \ell)$ -spider (a 1-subdivision of the in-star with  $\ell$  leaves) as a subgraph. They also conjectured that the bound on the minimum out-degree can be further improved to  $2\ell$ . In this note, we confirm their conjecture by showing that every directed graph with minimum out-degree at least  $2\ell$  contains a  $(2, \ell)$ -spider as a subgraph. This result is best possible, as the complete directed graph with  $2\ell$  vertices does not contain a  $(2, \ell)$ -spider.